Mathematik 8		
Bruchgleichungen	Lösungen	S. 124 / 3

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a)
$$\frac{12}{x} = \frac{6}{x-2} \mid \cdot x \cdot (x-2)$$
$$\frac{12 \cdot x \cdot (x-2)}{x} = \frac{6 \cdot x \cdot (x-2)}{x-2}$$
$$12(x-2) = 6x$$
$$12x-24 = 6x \mid -6x+24$$
$$6x = 24 \mid :6$$
$$x = 4$$

c)
$$\frac{x+8}{3x+3} + \frac{x+2}{2x+2} = 1$$

Bestimmung des Hauptnenners: 3x+3=3(x+1)

$$2x+2=2(x+1)$$

$$HN=2\cdot 3\cdot (x+1)$$

$$\frac{x+8}{3x+3} + \frac{x+2}{2x+2} = 1 \quad | \cdot 2 \cdot 3 \cdot (x+1)$$

$$\frac{(x+8) \cdot 2 \cdot 3 \cdot (x+1)}{3x+3} + \frac{(x+2) \cdot 2 \cdot 3 \cdot (x+1)}{2x+2} = 1 \cdot 2 \cdot 3 \cdot (x+1)$$

$$(x+8) \cdot 2 + (x+2) \cdot 3 = 6 \cdot (x+1)$$

$$2x+16+3x+6=6x+6$$

$$5x+22=6x+6 \quad | -5x-6$$

$$16 = x$$

e)
$$\frac{1}{x-1} - \frac{2}{x^2} = \frac{1}{x}$$

$$HN = x^2 \cdot (x-1)$$

$$\frac{1}{x-1} - \frac{2}{x^2} = \frac{1}{x} \quad | \quad \cdot x^2 \cdot (x-1)$$

$$\frac{1 \cdot x^2 \cdot (x-1)}{x-1} - \frac{2 \cdot x^2 \cdot (x-1)}{x^2} = \frac{1 \cdot x^2 \cdot (x-1)}{x}$$

$$x^2 - 2 \cdot (x-1) = x \cdot (x-1)$$

$$x^2 - 2x + 2 = x^2 - x \quad | \quad -x^2 + 2x$$

$$2 = x$$